## **Appendix B**

Appendix B presents an extended work for chapter 5 to demonstrate the potential of PDL to alter the SOP of an optical signal, consequently allowing orthogonality errors between two orthogonal multiplexed signals.

## **B.1 Orthogonality errors investigation and modelling results**

Since PDL has the potential to alter the state of polarisation [1] of an optical signal, any polarisation sensitive device with PDL, such as a coarse AWG [2], will have the potential to degrade the degree of orthogonality  $\theta$ , between two polarisation multiplexed signals SOP<sub>1</sub> and  $SOP<sub>2</sub>$  at the input of the device as shown in [Figure B-1.](#page-0-0) Since the PDL is aligned with the vertical axis of the transmission i.e. TM, it only reduces the vertical component of the SOPs vectors, resulting in modified SOP'<sub>1</sub> and SOP'<sub>2</sub> with degree of orthogonality θ', consequently allowing for orthogonality error figure of  $\theta$ - $\theta$ . In the scenario for which the device, such as the AWG, is located in the distribution point of a network, following a good condition fibre, the SOPs are random when reaching the device, although still mutually orthogonal [1], resulting in varying polarisation error.



<span id="page-0-0"></span>**Figure B-1 Degradation in orthogonality due to PDL, with representation in Jones space**

To demonstrate the effect of PDL on the reduction in orthogonality between the two polarisation multiplexed signals in the Gaussian AWG [2] passband at  $\lambda_2$ =1550 nm, the three fine wavelengths at  $\lambda_2^{-1}$ =1553.33,  $\lambda_2^{-9}$ =1550.12 nm and  $\lambda_2^{-16}$ =1547.32 nm, corresponding to the longest, centre and shortest wavelengths were employed. In the simulation, a polarisation controller was utilised at the input of the AWG to alter each wavelength SOP, consequently a first input SOP<sub>1</sub> was formed by azimuth  $\psi_1$  and ellipticity  $X_1$  angles and the corresponding Stokes parameters were measured at the output of the AWG using a Stokes measurement unit. Subsequently, for the same wavelength, an orthogonal input  $SOP<sub>2</sub>$  was also formed by setting the ellipticity and azimuth to  $X_2 = -X_1$  and  $\psi_2 = \psi_1 + 90$  respectively, and a second set of Stokes parameters enabled the orthogonality to be calculated using B.1 [1]. The entire Poincare sphere was scanned by varying the azimuth  $\psi_1$  and ellipticity  $X_1$  between -90° to 90° and -45° to 45° respectively in steps of 10°.

The scalar product, given by B.1 [1], of the two resultant vectors  $SOP'_{1}$  and  $SOP'_{2}$  is a measure of their orthogonality.

$$
2\theta = \arccos\left(\frac{\vec{S}_1' \times \vec{S}_2'}{|S_1'| \times |S_2'|}\right)
$$
 (B.1)

Where  $S'_1$  and  $S'_2$  are the Stokes representation of the two resultant vectors  $SOP'_1$  and  $SOP'_2$ respectively and the angle between the two vector in the sphere space is 2θ [3, 4]. Consequently, the angel between the two vectors in real space (Jones space) is measured by  $\theta$ .

[Figure B-2](#page-2-0) displays the orthogonality error mapping at coarse channel  $\lambda_2$ =1550 nm for the three wavelengths located at centre and both edges of the passband. As expected, due to increasing PDL at the edges of the passband, Figures B-2(a) and (c), for the longest and shortest wavelengths demonstrate up to 20° and 11° orthogonality errors respectively which could potentially result in significant crosstalk.

On the contrary, [Figure B-2](#page-2-0) (b) for the centre wavelength at  $\lambda_2^9 = 1550.12$  nm exhibits moderate orthogonality error of up to 4.5° due to low induced PDL at the centre of the passband [5].

Finally, Figures B-2(a), (b) and (c) suggest that an orthogonality error of approximately  $0^{\circ}$  can be achieved for all fine wavelengths in the scenario where the two SOP vectors are aligned with the device vertical and horizontal transmission modes. This is particularly true if the AWG is located in the OLT and as a result the orthogonality can be maintained.



<span id="page-2-0"></span>**Figure B-2** Effect of PDL on orthogonality error vs. operating wavelength. (a)  $\lambda_2$ <sup>1</sup>=1553.33 nm, **(b)**  $\lambda_2^9 = 1550.12$  nm, (c)  $\lambda_2^9 = 1547.32$  nm

To observe the tendency for the maximum orthogonality error in the passband, [Figure B-3](#page-3-0) displays the orthogonality error versus operating wavelength. As becomes evident from the figure the maximum error varies from approximately 0° for the fine wavelength  $\lambda_2$ <sup>11</sup>=1549.32 nm near the centre fine wavelength  $\lambda_2^{\circ}$  to more than 20° for the longest wavelength at  $\lambda_2$ <sup>16</sup> = 1553.33 nm. Similar results have been observed for all other coarse channels.



<span id="page-3-0"></span>**Figure B-3 Maximum orthogonality error versus operating wavelength in the passband**

## **B.2 References**

- [1] I. Tsalamanis, E. Rochat, M. C. Parker, and S. D. Walker, "Polarization Dependent Loss" and Temperature Fluctuations Effect on Degree of Orthogonality in Polarization Multiplexed Arrayed Waveguide Grating Based Distribution Networks," *IEEE Journal of Quantum Electronics*, vol. 41, pp. 945 - 950, 2005.
- [2] J. Jiang, C. L. Callender, C. Blanchetière, J. P. Noad, S. Chen, J. Ballato, and J. Dennis W. Smith, "Arrayed Waveguide Gratings Based on Perfluorocyclobutane Polymers for CWDM Applications," *IEEE Photonics Technology Letters*, vol. 18, pp. 370-372, 2006.
- [3] E. Rochat, S. Walker, and M. Parker, "C-band polarisation orthogonality preservation in 5Gb/s, 50µm multimode fibre links up to 3km," *Optics Express 'OSA'*, vol. 11, pp. 507- 514, 2003.
- [4] I. Tsalamanis, E. Rochat, S. D. Walker, and M. C. Parker, "Polarization orthogonality preservation in DWDM cascaded arrayed-waveguide grating networks," presented at Optical Fiber Communication and the National Fiber Optic Engineers Conference (OFC/NFOEC 2004), Los Angeles, USA, 2004.
- [5] Y. Shachaf, C.-H. Chang, P. Kourtessis, and J. M. Senior, "Multi-PON access network using a coarse AWG for smooth migration from TDM to WDM PON," *OSA Optics Express*, vol. 15, pp. 7840-7844, 2007.